

Modeling between-subject and within-subject variances in ecological momentary assessment data using mixed-effects location scale models

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Ecological momentary assessment and/or experience sampling methods are increasingly used in health studies to study subjective experiences within changing environmental contexts. In these studies, up to 30 or 40 observations are often obtained for each subject. Because there are so many measurements per subject, one can characterize a subject's mean and variance and can specify models for both. In this article, we focus on an adolescent smoking study using ecological momentary assessment where interest is on characterizing changes in mood variation. We describe how covariates can influence the mood variances and also extend the statistical model by adding a subject-level random effect to the within-subject variance specification. This permits subjects to have influence on the mean, or location, and variability, or (square of the) scale, of their mood responses. These mixed-effects location scale models have useful applications in many research areas where interest centers on the joint modeling of the mean and variance structure. Copyright © 2012 John Wiley & Sons, Ltd.

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1. Introduction

Modern data collection procedures, such as ecological momentary assessments (EMAs) [1, 2], experience sampling [3–5], and diary methods [6], have been developed to record the momentary events and experiences of subjects in daily life [6]. These procedures yield relatively large numbers of subjects and observations per subject, and data from these designs are sometimes referred to as intensive longitudinal data [7]. Such designs are in keeping with the ‘bursts of measurement’ approach described by Nesselroade and Schmidt McCollam [8], who called for such an approach in order to assess intra-individual variability. Nesselroade and Schmidt McCollam [8] noted that such bursts of measurement increase the research burden in several ways; however, they are necessary for studying intra-individual variation and to explain why subjects differ in variability rather than solely in mean level [6]. In this article, we describe data from a natural history study of adolescent smoking, using EMA, where interest was on determinants of the variation in the adolescents' moods.

In mental health research, EMA methods have been used in studying pediatric affective disorders [9], eating disorders [10, 11], drug abuse [12], schizophrenia [13, 14], borderline personality disorder [15], stress and anxiety [16, 17], and sexual abuse [18]. Similarly, in smoking research, some EMA studies include those studying relapse in people who are quitting smoking [19] and relapse among adolescent smokers [20] and those examining the urge to smoke [21], and our own EMA studies on adolescents [22, 23].

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Data from EMA studies are inherently multilevel with, for example, (level-1) observations nested within (level-2) subjects. Thus, linear mixed models (LMMs, aka multilevel or hierarchical linear models) are increasingly used for EMA data analysis [7, 24]. A basic characteristic of these models is the inclusion of random subject effects into regression models in order to account for the influence of subjects on their repeated observations. The variance of these random effects indicates the degree of variation that exists in the population of subjects, or the between-subject (BS) variance. Analogously, the error variance characterizes how much variation exists within a subject, or the within-subject (WS) variance. These variances are usually treated as being homogeneous across subject groups or levels of covariates.

In EMA studies, it is common to have up to 30 or 40 observations per subject, and this allows greater modeling opportunities than what conventional LMMs allow. In particular, one very promising extended approach is the modeling of both BS and WS variances as a function of covariates, in addition to their effect on overall mean levels. For example, if a smoker's mood is the outcome, then one can consider the effect of covariates on their mood level (e.g., how happy/sad they are on average), as well as on their variation in mood (e.g., how labile/erratic their mood is). Or, one can examine mood changes when a person smokes in terms of the mean (does mood improve?) and variance (does mood stabilize?) and what variables might be related to those smoking-related changes of mood level and variation. Thus, by allowing WS variance to be a function of covariates, we can more directly examine the hypothesis that smoking helps in regulating mood [25]. Indeed, in a recent review, Parrott [26] stated that mood vacillation and its relationship to nicotine dependency is an important topic for future research.

Recently, Hedeker *et al.* [27] described a mixed model for variance modeling of EMA data. Like all LMMs, this model allows covariates and a random subject effect to influence the mean response of a subject. However, this model also includes a log-linear structure for both the WS and the BS variances, allowing covariates to influence both sources of variation. Finally, a random subject effect is included in the WS variance specification. This permits the WS variance to vary at the subject level, above and beyond the influence of covariates on this variance. In this article, we more fully describe the mixed-effects location scale model of Hedeker *et al.* [27] and show how it can be used to model changes in mood levels and mood variation as a function of covariates. In particular, we examine the role of smoking on mood variation in adolescents. A standard software program (i.e., SAS PROC NL MIXED [SAS Institute Inc., Cary, NC, USA]) can be used to estimate the model parameters; a syntax example is available from the first author upon request.

2. Adolescent smoking, mood, and variability

Many prominent models of cigarette smoking maintain that smoking is reinforcing and that smoking can relieve negative affect (NA) [28, 29]. Indeed, both adults and adolescents often claim that smoking is relaxing and reduces emotional distress [28, 30]. However, although the relationship between mood and smoking has received substantial empirical attention for adult smokers, much less is known about the acute changes in mood with smoking among adolescents. The present study, with its focus on real-time assessments of mood and smoking among adolescents, helps shed light on this important topic.

Although there is substantial consensus among both smokers and researchers that smoking helps in regulating affect, most of the empirical work investigating the smoking–mood relationship has focused on the examination of changes in mean levels of mood with smoking. Surprisingly, although affect regulation inherently implies the modulation of variability in mood as well, the examination of variability in mood and smoking has largely been neglected. As Hertzog and Nesselroade [31] note, describing mean levels of variables is not always adequate for examining key features of developmental change. Variation also conveys important information about the phenomenon of interest. In the case of adolescent smoking and the development of dependence, variation in mood and mood changes may help better explain the development of tolerance. Examining individual variability may enhance our ability to predict changes in smoking behavior above and beyond what can be achieved by examining mean information alone.

Important, too, in the examination of mood and smoking, is the distinction between within-person and between-person variability. Kassel and colleagues [28, 32] have argued persuasively for the need to differentiate causal, within-person mechanisms from between-person data. Whether smoking relieves NA is essentially a within-person question; thus, analytic models need to similarly differentiate between WS and BS effects.

Much of the research on mood and smoking has also been limited to assessments of NA, while ignoring positive affect (PA). This neglect is particularly problematic given the theoretical importance of

differentiating between negative reinforcement models of smoking and positive reinforcement models, especially in the development of dependence among adolescents [33]. There is also considerable evidence to support the notion that PA and NA are distinct constructs, and not just opposite ends of a continuum [34, 35]. Thus, in the current study, we assessed both PA and NA.

Finally, there may well be individual differences in the extent to which adolescents' moods vary and whether they vary with smoking level. We hypothesized that level of smoking would affect mood variability. Following along the lines of the development of tolerance with dependence, we hypothesized that as smoking level or experience increased, variability in overall mood would decrease.

3. Adolescent smoking study

Data from a natural history study of adolescent smoking motivated the application of the location scale mixed model. Students included in this study were in either the 9th or the 10th grade at baseline, were 55.1% female, and self-reported on a screening questionnaire 6–8 weeks prior to baseline that they had smoked at least one cigarette in their lifetime. The majority (57.6%) had smoked at least one cigarette in the past month at baseline. We required for participation written parental consent and student assent. A total of 461 students completed the baseline measurement wave. The study utilized a multimethod approach to assess adolescents in terms of self-report questionnaires, a week-long time/event sampling method via palmtop computers (EMA), and in-depth interviews.

Here, we focus on the EMA data. Adolescents carried the handheld computers with them at all times during the seven-consecutive-day data collection period and were trained to both respond to random prompts from the computers and to event record (initiate a data collection interview) smoking episodes. Questions included ones about place, activity, companionship, mood, and other subjective items. The handheld computers date and time-stamped each entry. For the analyses reported, we treated the responses obtained from the random prompts. All in all, we obtained 14,105 random prompts from the 461 students with an approximate average of 30 prompts per student (range = from 7 to 71).

We considered two outcomes: measures of the subject's NA and PA at each random prompt. Both of these measures consisted of the average of several individual mood items, each rated from 1 to 10, that were identified via factor analysis. Specifically, PA consisted of the following items that reflected a subject's assessment of their positive mood before the prompt signal: I felt happy, I felt relaxed, I felt cheerful, I felt confident, and I felt accepted by others. Similarly, NA consisted of the following items assessing pre-prompt negative mood: I felt sad, I felt stressed, I felt angry, I felt frustrated, and I felt irritable. Over all prompts, and ignoring the clustering of the data, the marginal mean of PA was 6.797 (sd = 1.935), whereas the NA marginal mean was 3.455 (sd = 2.253).

Of interest is the degree of heterogeneity in these mood measures in terms of both WS and BS variations. Also, it is useful to examine whether certain covariates can explain some of the variation in these two sources of heterogeneity, over and above the influence of these covariates on the mean response. It is also reasonable to allow random subject effects both for the mean response (to allow for subjects with different average levels of mood) and for a subject's WS variance (to allow for different levels of mood consistency). The mixed location scale model, incorporates these considerations into a unified approach.

4. Mixed location scale model

Consider the following mixed-effects regression model for the affect measurement y , either NA or PA, of subject i ($i = 1, 2, \dots, N$ subjects) on occasion j ($j = 1, 2, \dots, n_i$ occasions):

$$y_{ij} = \mathbf{x}'_{ij}\boldsymbol{\beta} + v_i + \epsilon_{ij}, \quad (1)$$

where \mathbf{x}_{ij} is the $p \times 1$ vector of regressors (typically including a '1' for the intercept as the first element) and $\boldsymbol{\beta}$ is the corresponding $p \times 1$ vector of regression coefficients. The regressors can either be at the subject level, vary across occasions, or be interactions of subject-level and occasion-level variables. The random subject effect v_i indicates the influence of individual i on his or her repeated mood assessments. The population distribution of these random effects is usually assumed to be a normal distribution with zero mean and variance σ_v^2 . The errors ϵ_{ij} are also assumed to be normally distributed in the population with zero mean and variance σ_ϵ^2 and independent of the random effects. Here, σ_v^2 represents the BS variance, and σ_ϵ^2 is the WS variance.

To allow covariates (i.e., regressors) to influence the BS and WS variances, we can utilize a log-linear representation, as has been described in the context of heteroscedastic (fixed-effects) regression models [36,37], namely,

$$\sigma_{v_i}^2 = \exp(\mathbf{u}'_i \boldsymbol{\alpha}), \quad (2)$$

$$\sigma_{\epsilon_{ij}}^2 = \exp(\mathbf{w}'_{ij} \boldsymbol{\tau}). \quad (3)$$

The variances are subscripted with i and j to indicate that their values change depending on the values of the covariates \mathbf{u}_i and \mathbf{w}_{ij} (and their coefficients). The number of parameters associated with these variances does not vary with i or j . Both \mathbf{u}_i and \mathbf{w}_{ij} would usually include a (first) column of ones for the reference BS and WS variances (α_0 and τ_0), respectively. Thus, the BS variance equals $\exp \alpha_0$ when the subject-level covariates \mathbf{u}_i equal 0 and is increased or decreased as a function of these covariates and their coefficients $\boldsymbol{\alpha}$. Specifically, for a particular covariate u^* , if $\alpha^* > 0$, then the BS variance increases as u^* increases (and vice versa if $\alpha^* < 0$). Note that the exponential function ensures a positive multiplicative factor for any finite value of α , and so the resulting variance is guaranteed to be positive. The WS variance is modeled in the same way, with the exception that both time-varying and subject-varying covariates can influence the WS variance. For this reason, the covariate vector is indicated as \mathbf{w}_{ij} for the WS variance. Thus, this model allows both subject-varying and time-varying covariates to influence the WS variance but only subject-varying variables to influence the BS variance. The coefficients in $\boldsymbol{\alpha}$ and $\boldsymbol{\tau}$ indicate the degree of influence on the BS and WS variances, respectively, and the ordinary random intercept model is obtained as a special case if $\boldsymbol{\alpha} = \boldsymbol{\tau} = 0$ for all covariates in \mathbf{u}_i and \mathbf{w}_{ij} (i.e., excluding the reference variances α_0 and τ_0).

We can further allow the WS variance to vary across subjects, above and beyond the contribution of covariates, namely,

$$\sigma_{\epsilon_{ij}}^2 = \exp(\mathbf{w}'_{ij} \boldsymbol{\tau} + \omega_i), \quad (4)$$

where the random subject (scale) effects ω_i are distributed in the population of subjects with mean 0 and variance σ_{ω}^2 . The idea for this is akin to the inclusion of the random (location) effects in Equation (1), namely, covariates do not account for all of the reasons that subjects differ from each other. The v_i parameters in Equation (1) indicate how subjects differ in terms of their means, and the ω_i parameters in Equation (4) indicate how subjects differ in variation, beyond the effect of covariates. Notice that taking logs in Equation (4) yields $\log(\sigma_{\epsilon_{ij}}^2) = \mathbf{w}'_{ij} \boldsymbol{\tau} + \omega_i$, which indicates that if the distribution of ω_i is specified as normal, then the random effects serve as lognormal subject-specific perturbations of the WS variance. In other words, the WS variances follow a lognormal distribution at the individual level. The skewed, nonnegative nature of the lognormal distribution makes it a reasonable choice for representing variances, and it has been used in many diverse research areas for this purpose [38–42].

In this model, v_i is a random effect that influences an individual's mean, or location, and ω_i is a random effect that influences an individual's variance, or (square of the) scale. Thus, we dub the model with both types of random effects as a mixed-effects location scale model. These two random effects are correlated with covariance parameter $\sigma_{v\omega}$. This covariance parameter indicates the degree to which the random location and scale effects are associated with each other. Details on estimation of model parameters can be found in the work by Hedeker *et al.* [27]; a nice feature of the model is that a standard software program (i.e., SAS PROC NLMIXED) can be used for estimation.

Visually, Figure 1 presents the pertinent details of the model. In this figure, the solid horizontal line depicts the average across all subjects, and dotted lines represent the lines of two subjects. Data points for these two subjects are also included in the plot. In a given dataset, there will be as many dotted lines as there are subjects, but for simplicity, here, we only plot two subjects. Also, for simplicity, consider all covariates as subject varying only. $\boldsymbol{\beta}$ represents the effect of covariates \mathbf{x} on the mean response; this effect influences the solid line by either raising or lowering it as a function of the covariates. Each dotted line is indicative of a person's random location effect v_i , which indicates how a subject deviates from the mean response. In the figure, one subject is above and another subject is below the mean line. The heterogeneity in these dotted lines is indicative of BS variance: if the dotted lines are close together, then there is not much subject heterogeneity; conversely, if the dotted lines are spread out, then more heterogeneity is indicated. The effect of covariates \mathbf{u} on this heterogeneity is represented in the model as $\boldsymbol{\alpha}$. The degree of variation of a person's data points around their line is the WS variance. If the points are

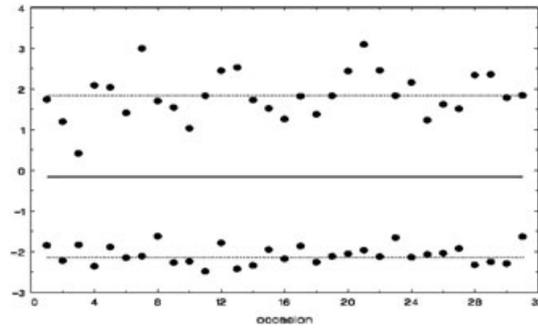


Figure 1. Mean response (solid line), mean deviations of two subjects (dotted lines), and data across occasions for these two subjects (solid dots).

quite close to a subject's line, then that subject has low WS variance (i.e., the lower subject in the figure). Conversely, if a subject's data points vary greatly around that person's line, then more WS variation is indicated (i.e., the upper subject in the figure). Covariates w influence this WS variation through the coefficients τ . Finally, the model posits that covariates do not explain all of WS variance by including the random scale effect ω_i .

5. Results

To begin, we fit models for NA and PA without any covariates. Table I lists the parameter estimates of these models. Mean PA and NA scores are estimated to be approximately 6.8 and 3.5, respectively. These estimates account for the clustering of the data within subjects and allow for the fact that subjects have different numbers of occasions. In terms of the variance estimates, there is considerable heterogeneity of both location and scale between subjects. For both PA and NA, the estimates of α_0 (location variation) and σ_ω^2 (scale variation) greatly exceed their standard error estimates. Thus, subjects differ in terms of their PA and NA mean level *and* level of variation. Interestingly, the estimates for PA are rather smaller than their NA counterparts. This suggests that there is more subject heterogeneity in both mean and variation for NA, relative to PA.

Turning to the covariance ($\sigma_{v\omega}$) estimates, we can see that these are also relatively large and of opposite sign for PA and NA. For NA, the positive covariance indicates that subjects who are high in terms of their NA mean also exhibit greater variation in NA. Thus, subjects with relatively poor moods (higher NA) fluctuate more in their mood. This could reflect the notion that better moods (less NA) may be more 'trait-like' and not as reactive to different situational cues. Alternatively, this positive association might reflect a floor effect of measurement. Namely, as noted, the marginal mean of NA is about 3.5, or relatively low and towards the minimum of this scale. Thus, subjects who are lower than average have relatively less room to vary downward than those who are above average. Conversely, the negative covariance for PA indicates that subjects who are relatively high in terms of their mean PA are less varied across prompts in their PA responses. Again, this could suggest that more positive moods reflect trait-like positivity, or this could be a ceiling effect of measurement, because the marginal mean of PA is about 6.8, or towards the maximum value for this scale. Thus, one might argue that subjects with greater-than-average PA have relatively less room for upward movement and so less variation.

Table I. Positive and negative affect—maximum likelihood estimates and se.*				
Parameter	Positive affect		Negative affect	
	estimate	se	estimate	se
Mean β_0	6.779	.058	3.482	.071
WS variance τ_0	.622	.036	.741	.047
BS variance of location α_0	.367	.069	.793	.069
BS variance of scale σ_ω^2	.518	.039	.963	.069
Covariance $\sigma_{v\omega}$	-.386	.048	.765	.080

* $p < .001$ for null hypothesis tests of all model parameters (i.e., H_0 : parameter = 0).
se, standard errors; WS, within-subject; BS, between-subject.

Finally, one can reexpress the parameter estimates to yield BS and WS estimates in their original scale. For BS variance, these are simply equal to $\exp(\alpha_0)$, yielding 1.443 and 2.210 for PA and NA, respectively. For WS variance, the translation of $\exp(\tau_0 + .5\sigma_\omega^2)$ [27] gives 2.413 and 3.396 for PA and NA, respectively. Thus, as mentioned earlier, more variation, both BS and WS, is seen for NA than for PA. These estimates can be further expressed as an intraclass correlation, namely the BS variance divided by the sum of the BS and WS variances. This yields values .374 and .394 for PA and NA, respectively, indicating that the data are moderately correlated within subjects for both mood variables.

To examine the effect of smoking level on mood, we augmented the models for PA and NA with the subject-level covariate `Smoker`, an indicator of whether the subject is a current smoker (coded no = 0 or yes = 1). This was determined on the basis of whether the subject provided at least one smoking event during the week-long data collection period. Of the 461 adolescents, 234 (51%) did provide a smoking event, whereas 227 (49%) did not. We also included the variable `Male` (coded 0 = female or 1 = male) to control for gender effects on mood. In this study, there were 254 women (55%) and 207 men (45%). Table II presents the results of these analyses of PA and NA.

In terms of the means, men have significantly higher PA ($\hat{\beta}_1 = .296, p < .01$) and significantly lower NA ($\hat{\beta}_1 = -.603, p < .001$) than women. Also, smokers have significantly higher NA levels ($\hat{\beta}_2 = .283, p < .04$) than nonsmokers. For the WS variance, men elicit less varied responses on both PA and NA ($\hat{\tau}_1 = -.276$ and $-.453$, respectively, with $p < .001$ for both). Additionally, in terms of the BS variance of NA, men are less varied as a group than women ($\hat{\alpha}_1 = -.319, p < .005$). For smokers, there is a significant positive effect on WS variance of NA ($\hat{\tau}_2 = .238, p < .01$), indicating that smokers give more varied NA responses than nonsmokers. The scale variance and scale-location covariance terms remain highly significant in both models, with similar interpretations as previously described.

The aforementioned model collapses all subjects with a smoking event into a single group. A closer examination of the effect of smoking considers a subject's smoking level and not just whether they are a current smoker. For this, we created a variable `Psmk` equaling the proportion of occasions (both random prompts and smoking events) that were smoking events for a subject. In the sample of 461, the average number and median of random prompts equaled 30, with a range of 7–71. Of the 234 subjects that provided a smoking event during the measurement period (approximately 1 week), the average was 5, the median was 3, and the range was from 1 to 42 reported events. The quartiles of the variable `Psmk` equaled .049 (25%), .081 (50%), and .179 (75%), reflecting a moderate degree of variation in the level of smoking among these adolescents. By including both `Smoker` and `Psmk` as regressors, we are estimating a piecewise linear relationship in which the slope for `Smoker` reflects the difference between

Table II. Mixed location scale model of positive and negative affect, $N = 461$ and $\sum n_i = 14, 105$, maximum likelihood estimates, se, and p -values.

Parameter	Positive affect			Negative affect		
	estimate	se	$p <$	estimate	se	$p <$
Mean						
Intercept β_0	6.741	.094	.001	3.609	.118	.001
Male β_1	.296	.114	.01	-.603	.136	.001
Smoker β_2	-.188	.115	.10	.283	.136	.04
WS variance						
Intercept τ_0	.706	.060	.001	.824	.077	.001
Male τ_1	-.276	.072	.001	-.453	.093	.001
Smoker τ_2	.078	.071	.27	.238	.092	.01
BS variance						
Intercept α_0	.292	.102	.004	.908	.067	.001
Male α_1	-.103	.121	.400	-.319	.113	.005
Smoker α_2	.198	.120	.100	.111	.110	.31
Scale						
BS variance of scale σ_ω^2	.506	.039	.001	.908	.065	.001
Covariance $\sigma_{\nu\omega}$	-.361	.046	.001	.661	.073	.001

se, standard errors; WS, within-subject; BS, between-subject.

Table III. Mixed location scale model of positive and negative affect, $N = 461$ and $\sum n_i = 14, 105$, maximum likelihood estimates, se, and p -values.

Parameter	Positive affect			Negative affect		
	estimate	se	$p <$	estimate	se	$p <$
Mean						
Intercept β_0	6.740	.094	.001	3.607	.117	.001
Male β_1	.299	.114	.01	-.599	.135	.001
Smoker β_2	-.192	.147	.19	.483	.175	.006
Psmk β_3	.018	.742	.98	-1.530	.791	.054
WS variance						
Intercept τ_0	.704	.059	.001	.820	.077	.001
Male τ_1	-.272	.071	.001	-.444	.092	.001
Smoker τ_2	.167	.090	.07	.427	.117	.001
Psmk τ_3	-.693	.430	.11	-1.446	.554	.01
BS variance						
Intercept α_0	.293	.102	.004	.800	.100	.001
Male α_1	-.115	.123	.35	-.319	.115	.006
Smoker α_2	.152	.156	.33	.192	.140	.17
Psmk α_3	.370	.812	.65	-.657	.653	.31
Scale						
BS variance of scale σ_ω^2	.503	.038	.001	.893	.064	.001
Covariance $\sigma_{\nu\omega}$	-.356	.047	.001	.647	.071	.001

se, standard errors; WS, within-subject; BS, between-subject.

low-level smokers (i.e., those with the lowest value of Psmk) and nonsmokers, whereas the slope for Psmk reflects the slope only among smokers. Table III lists the results by using these two smoking-related variables, plus gender, in the mean model, as well as the models of WS and BS variances, of PA and NA.

First, comparing the models with and without the Psmk variable yields likelihood ratio tests results of $\chi^2_3 = 3$ and 8 for PA and NA, respectively. Thus, smoking level does not significantly alter the results for PA ($p = .39$) but does for NA ($p < .05$). For NA, in terms of the mean, the low-level effect of Smoker is positive and significant ($\hat{\beta}_2 = .483, p < .006$), whereas the effect of smoking level (Psmk) is negative and marginally significant ($\hat{\beta}_3 = -1.530, p < .054$). This suggests that low-level smokers have the highest NA levels, relative to nonsmokers and higher-level smokers. Also, a similar relationship is apparent in terms of the WS variance of NA, with a significant positive effect of low-level smoking ($\hat{\tau}_2 = .427, p < .006$) coupled with a significant negative effect of smoking level ($\hat{\tau}_3 = -1.446, p < .01$). Thus, low-level smokers are more varied in their NA responses relative to nonsmokers and higher-level smokers. A similar, although nonsignificant, pattern of results is observed for the effect of smoking on the WS variance of PA. These results support the notion that the mood stabilization effect of smoking, at least in terms of NA, increases with the level of smoking.

6. Discussion

This article has presented a location-scale mixed model that augments the mean model with submodels of the BS and WS variances. Covariates can be included in each of these submodels. Relative to the standard mixed model, this augmented approach can be useful to identify predictors of both WS and BS variations and to test hypotheses about these variances. Also, by including a random subject effect on the WS variance, this model can examine the degree to which subjects are heterogeneous in terms of their variation on the outcome variable, over and above the effects of covariates. The random scale effects are further allowed to be correlated with the usual random location effects. Our examples with NA and PA clearly show that subjects are quite heterogeneous in terms of their mood variation and also that there is appreciable correlation between a subject's mood level (location) and their volatility (scale).

For both NA and PA, worse mood levels (higher on NA and lower on PA) were associated with greater mood volatility. Additionally, in terms of NA, we observed a positive curvilinear effect of smoking level on the mean and WS variance.

Modern data collection procedures, such as EMA and/or real-time data captures, are increasingly used in many research areas. These approaches often provide a fair amount of both WS and BS data and so allow the opportunity for modeling both WS and BS variances as a function of covariates. The question of how much WS and BS data are necessary for variance modeling purposes is difficult to address definitively. For random coefficient models, Longford [43] noted the difficulty with providing general guidelines about the degree of complexity, for the variation part of a model, that a given dataset could support. This would seem to be true here as well. Carrying out some simulations with relatively small sample sizes (e.g., 20 subjects with five observations each) gives the general impression that the primary issue is that the estimation algorithm does not often converge, but instead, has estimation difficulties of one sort or another, in small sample situations. Clearly, more work is necessary in this area.

In this paper, we have presented the mixed location-scale model for a continuous normal outcome. We have also developed this approach for ordinal outcomes [44]. In the ordinal approach, we extend the mixed-effects logistic regression model of Hedeker and Gibbons [45] by including the log-linear modeling of BS and WS variances, as well as the random scale effect. Also, as with the model presented in this paper, SAS NLMIXED can be used to estimate the parameters of the ordinal location-scale model, and Hedeker *et al.* [44] includes sample syntax.

As this is a relatively new modeling technique, certain limitations and cautions should be mentioned. Our model assumes that the random location effects are normally distributed and that the random scale effects are lognormally distributed. It is unclear how robust this model is to violations of these assumptions. To some extent, this can be examined empirically using the approach of Liu and Yu [46] for models with non-normal random effects. Also, attention should be paid to outliers and influential observations, as these might have undue effects on estimation of the model parameters, especially the variance parameters.

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